

UNIVERSITY OF ILLINOIS
DIGITAL COMPUTER

LIBRARY ROUTINE R 1 - 116

TITLE Square Root (DOI or SADOI)
TYPE Closed
NUMBER OF WORDS 9
TEMPORARY STORAGE 0, 1, 2
ACCURACY $\pm 2^{-39}$
DURATION 1.3 n milliseconds, where n is defined by
 $[(1 - \sqrt{a}) / (1 + \sqrt{a})]^{2n} < 2^{-39}$
DESCRIPTION The argument a may consist of 39 digits or of 78 digits.
The sign and 39 most significant digits should be in A
but may be in address 1 if the routine is entered at the
right hand side of the first word instead of at the normal
left hand side. The 39 least significant digits (if any)
must be in address 0.

The program uses Newton's method by means of the relations

$$x_0 = a/2 + 1/2$$

$$x_{n+1} = x_n + [a/x_n - x_n] / 2$$

and convergence is assumed to have occurred when

$$(a/x_n) - x_n = 2(x_{n+1} - x_n) \geq 0.$$

NOTE

The Illiac will stop if $a < 0$ or if $a = 1 - 2^{-39}$.

Rt. 7/20/59

DATE Oct. 23, 1953 Rt. 3/18/58

CODED BY D. J. Wheeler

APPROVED BY J. P. Nash

| LOCATION | ORDER | | NOTES PAGE 1 |
|----------|----------|--------|----------------------|
| | 00K (R1) | | |
| 0 | 40 1F | | Store a |
| | K5 F | | |
| 1 | 42 8L | | Plant link |
| | 51 1F | | |
| 2 | 10 1F | | $x_0 = a/2 + 1/2$ |
| | SJ F | | |
| 3 | 40 2F | From 7 | to 2F |
| | 50 F | | |
| 4 | L5 1F | | a to A and Q |
| | 66 2F | | |
| 5 | S5 F | | |
| | L0 2F | | $x_{n+1} - x_n$ to A |
| 6 | 10 1F | | |
| | 36 8L | | End test |
| 7 | L4 2F | | |
| | 26 3L | | Re-enter loop |
| 8 | L5 2F | | \sqrt{a} to A |
| | 22 F | by 1 | Link |